MATLAB for REU/REV 2011

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l assume

- Basic knowledge of computer
 - File system (create files, directories, etc.)
 - Use a text editor, like notepad (not word processor)
- Basic knowledge of linear algebra
 - scalar versus matrix
 - matrix operations

In two hours you will

- be able to perform arithmetic operations
- have an understanding of vectorized operations
- be able to write simple program and functions
- plot graphs
- hungry enough to enjoy your lunch

What is MATLAB?

- MATLAB = **MAT**rix **LAB**oratory
- High-level programming language
 - Easy to learn, make abstraction of internal computer machinery
- Command line based
 - Powerful, but not as intuitive as other programs

Open MATLAB

- Windows
 - Start -> All Programs -> Matlab -> Matlab
- Linux/Mac
 - Open a terminal and write
 - \$ matlab &

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Where are you?

- Change the current folder
 - One project one folder
 - >> cd *path*
 - Use the ... right next to the *current folder* address

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MATLAB 7.11.0 (R2010b)

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Getting started

- Use MATLAB as an expensive calculator
 - >> 1 + 2
 - >> 5 4
 - >> 4 * 4
 - >> 10 / 5
 - >> 2^9
 - >> log(100)

Wait a minute

- log₁₀(100)=2 why do I get 4.6?
- >> help log
 - The default is $log_{e}(X)$ if I want $log_{10}(X)$ I should use
 - >> log10(X)

Single most important command

- >> help <what you are looking for>
- and its companion
- >> lookfor <what you are looking for>

How MATLAB is different from a pocket calculator?

- You can save the output and use it later
- >> radius = 4/2
- >> area = pi * radius^2
- Exercise
 - Define a variable "circum" which computer the circumference of a circle

Script file

- Prevent writing the same command over and over
- Good to keep track of what you do
- Ensure replicability, essential in science
- File -> New -> Script

Script file

% This is a commentary. Everything after % is not interpreted by Matlab % Compute area and circumference of circle, given the radius

rad=input('radius = '); % Input from command window area = pi * rad^2 % No semicolon = output to command window circum = 2*pi*rad

- Save it into the working directory under areaCirc.m
 - File -> Save (in the text editor window)
- To execute it type its file name without the ".m"
 - avoid unusual characters (!@#\$%^&*~\+=.,<>{})
 - avoid space

Matrix and vectors

- Row vector
 - >> x=[1 2 3] or
 - >> x=[1,2,3]
 - >> z=[2 1 sin(pi)]
 - >> w=[x z]
- Column vector
 - >> y=[2;1;5]

Matrix and vector operations

- Addition
 - >> a=x+z
- Multiplication
 - >> a=x*z
 - oups!
 - >> a=x.*z
 - >> b=x*y

Creation of vectors

- You cannot always afford to enter every value manually
 - Vector of one to one thousand by increment of one
 - >> x=[1 2 3 4 5 6 ... 1000];
 - Shortcut
 - >> x=linspace(1,1000,1000);
 - or
 - >> x=1:1:1000;
 - or
 - >> x=1:1000;

Exercise

- Create a row vector 'b' 36 elements from 1 to 14
- Create a column vector 'c' of 14 elements from 14 to 30
- Combine vector b and c in a single row vector 'd'
 - Remember your linear algebra and use help/lookfor if you need it.

Simple plot

- Create a vector for the x axis
- >> x=0:0.1:4;
- Calculate the corresponding y values
- >> y=x.^3.*sin(x).^2;
 - No need for a loop!
- plot the figure
- >>plot(x,y)
- Axis labeling
- >>xlabel('x')
- >>ylabel('y')
- Add a title
- >> title('First figure')

Save the graph

- Command line option
- >> saveas(gcf,'test.eps','eps')
- >> saveas(gcf,'test.bmp','bmp')
- Click and follow instructions
 - File -> Save as ...

Exercise

- Write a script file that plots area and circumference of a circle as a function of its radius. Use the following syntax to create a graph with two plots in different colors and symbols: plot(x,y,'r',x,z,'+')
 - You may want to learn more about the command legend



Matrix 2D

- Matrix
 - >> A = [1 2 3 ; 4 5 6 ; 7 8 9]
 - Check the orientation (row filled first)
- Shortcut to create matrix
 - >> B=zeros(3,3)
 - zeros(number of rows, number of column)
 - >> C=ones(3,3)
- Access a specific element (2nd row, 3rd column)
 - >> A(2,3)
- Access a single dimension
 - >> A(:,3)

Simple matrix operation

- Transpose
 - D=A'
- Multiplication
 - >> A*D
 - Watch for dimension matching
- Element-wise multiplication
 - E=A.*D

Leslie matrix

Age structured population with 4 classes $n_0 n_1 n_2 n_3$ Next time step there will be production of newborn n_0 $n_0(t+1) = \sum_{i=0}^{3} f_i n_i(t)$

There will be aging of everybody that survive

$$n_i(t+1) = s_{i-1} n_{i-1}(t)$$

How do we study the population age structure?

Leslie matrix
$$n_0(t+1) = \sum_{i=0}^{3} f_i n_i(t) \qquad n_i(t+1) = s_{i-1} n_{i-1}(t)$$

$$\begin{bmatrix} n_0(t+1) \\ n_1(t+1) \\ n_2(t+1) \\ n_3(t+1) \end{bmatrix} = \begin{bmatrix} f_0 & f_1 & f_2 & f_3 \\ s_0 & 0 & 0 & 0 \\ 0 & s_1 & 0 & 0 \\ 0 & 0 & s_2 & 0 \end{bmatrix} \begin{bmatrix} n_0(t) \\ n_1(t) \\ n_2(t) \\ n_3(t) \end{bmatrix}$$

 $\boldsymbol{n}(t+1) = \boldsymbol{L} \boldsymbol{n}(t)$

Lets say we have f, s and n

$$\begin{vmatrix} n_0(1) \\ n_1(1) \\ n_2(1) \\ n_3(1) \end{vmatrix} = \begin{vmatrix} 1.6 & 1.5 & 0.25 & 0.1 \\ 0.8 & 0 & 0 & 0 \\ 0 & 0.5 & 0 & 0 \\ 0 & 0 & 0.25 & 0 \end{vmatrix} \begin{vmatrix} 60 \\ 50 \\ 40 \\ 50 \end{vmatrix}$$

Find the population distribution for the next generation.

Find the population age structure after a million generations (Remember your linear algebra!)

Eigenvalues - eigenvectors

- Eigenvalue of a matrix
 - >>eig(L)
- Eigenvalue and eigenvector
 - >> [V,D] = eig(L)

Functions

- eig is a function
- [output1, output2, ...] = functionName(input1, input2, ...)
- A function is a black box that (usually) does what we want
- We can create our own function for everything that we may have to repeat

Simple function example

File -> New -> Function

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Simple function example

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| <pre>1 function [sum] = addition(a,b) 2</pre> | | | | | | | |
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Use your new function

- Save the function in the working directory
 - name of the function should be the name of the file
- Call your function like any other function
 - >> addition(2, 2)
 - >> result = addition(2, 2)

Read file

- Download lvData.csv from website http://nimbios.org/~xavier/REU/
- Read csv file
- >> M=csvread('lvData.csv');
- Plot your column 1 as a function of column 2

- for
 - Repeat something a fix number of time
- if
 - Conditional statement
- while
 - Repeat operation until a specific state

- To repeat operation several time
- Example: sum all integer from 1 to 10
- >> j=0;
- >> for i=1:10
- >> j=j+i;
- >> end
- If you are mathematician, you know that

$$\sum_{i=i}^{N} i = \frac{N(N+1)}{2}$$

- Exercise find the first 100 number of the Fibonacci sequence
- $F_{i} = F_{i-1} + F_{i-2}$
- $F_1 = F_2 = 1$
- Hint: use a vector to store your answer

• Simulate a logistic growth and write a function that return the time series for a given r (growth rate) and for a given number of iterations

$$x_t = r x_{t-1} (1 - x_{t-1})$$

- Hint: use a vector to store your answer
- Hint2: x1 should be near one, but not equal to one and r should be between 1 and 4

- Conditional statement
- Is the number odd or even?
- >> x=4;
- >> if (mod(x,2) == 0)
- >> 'even'
- >>else
- >> 'odd'
- >>end

- Conditions
- a == b is a equal to b
- a < b is a smaller than b
- a > b is a greater then b
- a <= b is a smaller or equal than b
- a >= b is a greater or equal than b
- a ~= b is a different than b

- Combination of conditions
- A & & B True if A and B are true
- A || B True if at least A or B is true
- xor(A,B) True only if one of A or B is true (exclusive)

• Exercise: write a function that return if a number is positive and odd (single answer).

- A mix of repetition and condition
- >> i=10;
- >> while (i > 0)
- >> i=i-1;
- >> end

Synthesis problem

4

r

 Write a script that use your function for the logistic growth to study the behavior of population size at 'equilibrium'

Population Size

Synthesis problem

- 2<= r <= 4 (0.001 increment)
- 1000 iteration burn in for a 10 000 iteration simulation
- Check the function unique
- Plot dot and not lines

Wrap up

- help is the most useful command
- lookfor is also very useful
- If not there is Internet (look for Matlab and your question/keywords)
- Cheat sheet
 - Find one first, them make your own
- Always use an editor to track your work

Thank you!